## Warm Up <br> 9/13/22



The car is in this box


The car is not in this box


The car is not in box 1

One of the boxes contains a car.
On each box there is a statement, exactly one of which is true. Where is the car? Justify your reasoning.

Justify Reasoning Prove the Linear Pair Theorem. Given: $\angle M J K$ and $\angle M J L$ are a linear pair of angles. Prove: $\angle M J K$ and $\angle M J L$ are supplementary.


Complete the proof by writing the missing reasons. Choose from the following reasons.

Angle Addition Postulate Definition of linear pair
Substitution Property of Equality

| Statements | Reasons |
| :--- | :--- |
| 1. $\angle M J K$ and $\angle M J L$ are a linear pair. | 1. |
| 2. $\overrightarrow{J L}$ and $\overrightarrow{J K}$ are opposite rays. | 2. |
| 3. $\overrightarrow{J L}$ and $\overrightarrow{J K}$ form a straight line. | 3. Definition of opposite rays |
| 4. $\mathrm{m} \angle L J K=180^{\circ}$ | 4. Definition of straight angle |
| 5. $\mathrm{m} \angle M J K+\mathrm{m} \angle M J L=\mathrm{m} \angle L J K$ | 5. |
| 6. $\mathrm{m} \angle M J K+\mathrm{m} \angle M J L=180^{\circ}$ | 6. |
| 7. $\angle M J K$ and $\angle M J L$ are supplementary. | 7. Definition of supplementary angles |

## Proof of Linear Pair Theorem.

Given: $\angle M J K$ and $\angle M J L$ are a linear pair of angles. Prove: $\angle M J K$ and $\angle M J L$ are supplementary.


| Statements | Reasons |
| :--- | :--- |
| 1. $\angle M J K$ and $\angle M J L$ are a linear pair. | 1. Given |
| 2. $\overrightarrow{J L}$ and $\overrightarrow{J K}$ are opposite rays. | 2. Definition of Linear Pair |
| 3. $\overrightarrow{J L}$ and $\overrightarrow{J K}$ form a straight line. | 3. Definition of Opposite Rays |
| 4. $m \angle L J K=180^{\circ}$ | 4. Definition of Straight Angles |
| 5. $m \angle M J K+m \angle M J L=m \angle L J K$ | 5. Angle Addition Postulate |
| 6. $m \angle M J K+m \angle M J L=180^{\circ}$ | 6. Substitution Property of Equality |
| 7. $\angle M J K$ and $\angle M J L$ are supplementary | 7. Definition of Supplementary Angles |

## Proof of Vertical Angles Theorem

Vertical Angles Theorem
Given: $\angle 1$ and $\angle 3$ are vertical angles.
Prove: $\angle 1 \cong \angle 3$


| Statements | Reasons |
| :--- | :--- |
| 1. | 1. |
| 2. | 2. |
| 3. | 3. |
| 4. | 4. |
| 5. | 5. |
| 6. | 6. |
| 7. | 7. |

Proof of Vertical Angles Theorem.

Given: $\angle 1$ and $\angle 3$ are vertical angles.
Prove: $\angle 1 \cong \angle 3$


| Statements | Reasons |
| :--- | :--- |
| 1. $\angle 1$ and $\angle 3$ are vertical | 1. Given |
| 2. $\angle 1$ and $\angle 2$ are a linear pair <br> $\angle 2$ and $\angle 3$ are a linear pair | 2. Given (from diagram) |
| 3. $\angle 1$ and $\angle 2$ are supplementary <br> $\angle 2$ and $\angle 3$ are supplementary | 3. Linear Pair Theorem |
| 4. $m \angle 1+\mathrm{m} \angle 2=180$ |  |
| $\quad m \angle 2+\mathrm{m} \angle 3=180$ | 4. Definition of Supplementary |
| $5 . m \angle 1+\mathrm{m} \angle 2=m \angle 2+\mathrm{m} \angle 3$ | 5. Transitive Property of Equality |
| $6 . m \angle 1=m \angle 3$ | 6. Subtraction Property of Eq. |
| 7. $\angle 1 \cong \angle 3$ | 7. Definition of Congruence |

Given: $p \| q$
Prove: $m \angle 4=m \angle 6$


Choose from the following reasons. You may use a reason more than once.

- Same-Side Interior Angles Postulate
- Definition of Supplementary Angles
- Given
-Linear Pair Theorem
- Subtraction Property of Equality
- Substitution Property of Equality

| Statements |  |
| :--- | :--- |
| 1. $p \\| q$ | Reasons |
| 2. $\angle 4$ and $\angle 5$ are <br> supplementary | 1. |
| 3. $m \angle 4+m \angle 5=180^{\circ}$ | 3. |
| 4. $\angle 5$ and $\angle 6$ are a linear pair | 4. |
| 5. $\angle 5$ and $\angle 6$ are <br> supplementary | 5. |
| 6. $m \angle 5+m \angle 6=180^{\circ}$ | 6. |
| 7. $m \angle 4+m \angle 5=m \angle 5+m \angle 6$ |  |
| 8. $m \angle 4=m \angle 6$ | 7. |

## Proof of Interior Angles Theorem

Given: $p \| q$

Prove: $m \angle 4=m \angle 6$

| Statements | Reasons |
| :--- | :--- |
| 1. $p \\| q$ | 1. Given |
| 2. $\angle 4 \& \angle 5$ are supplementary | 2. Same-Side Interior Angles Postulate |
| 3. $m \angle 4+m \angle 5=180^{\circ}$ | 3. Definition of Supplementary Angles |
| 4. $\angle 5 \& \angle 6$ are a linear pair | 4. Given |
| 5. $\angle 5 \& \angle 6$ are supplementary | 5. Linear Pair Theorem |
| 6. $m \angle 5+m \angle 6=180^{\circ}$ | 6. Definition of Supplementary Angles |
| 7. $m \angle 4+m \angle 5=m \angle 5+m \angle 6$ | 7. Substitution Property of Equality |
| 8. $m \angle 4=m \angle 6$ | 8. Subtraction Property of Equality |

Prove the Alternate Exterior Angles Theorem
Given: $p \| q$
Prove: $\angle 1 \cong \angle 7$


| Statements | Reasons |
| :--- | :--- |
| $1 . p \\| q$ | 1. |
| 2. | 2. |
| 3. | 3. |
| 4. | 4. |
| 5. | 5. |

## Proof of Exterior Angles Theorem

Given: $p \| q$

Prove: $m \angle 1=m \angle 7$


## Reasons

## Statements

1. $p \| q$
2. $m \angle 1=m \angle 3$
3. given
4. $m \angle 3=m \angle 5$
5. $m \angle 5=m \angle 7$
6. $m \angle 1=m \angle 7$
7. Vertical Angles Theorem
8. Vertical Angles Theorem
9. Alternate Interior Angles Theorem
10. Transitive Property of Equality

Write a proof in two-column form for the Corresponding Angles Theorem.
Given: $p \| q$
Prove: $\mathrm{m} \angle 1=\mathrm{m} \angle 5$

| Statements | Reasons |
| :--- | :--- |
|  |  |
|  |  |
|  |  |
|  |  |



Proof of Corresponding Angles Theorem
Given: $p \| q$
Prove: $m \angle 1=m \angle 5$


| Statements | Reasons |
| :--- | :--- |
| 1. $p \\| q$ | 1. given |
| 2. $m \angle 1=m \angle 3$ | 2. Vertical Angles Theorem |
| 3. $m \angle 3=m \angle 5$ | 3. Alternate Interior Angles Theorem |
| 4. $m \angle 1=m \angle 5$ | 4. Substitution Property of Equality |

