

Coordinate proof of a trapezoid

Name _____

Use Coordinate Geometry to prove that quadrilateral $ABCD$ is a trapezoid given the vertices $A(0, 5)$, $B(5, 0)$, $C(7, 4)$ and $D(4, 7)$.

Show that exactly one pair of opposite sides is parallel, which means their slopes are the same.

Formula for the slope $m = \frac{y_2 - y_1}{x_2 - x_1}$

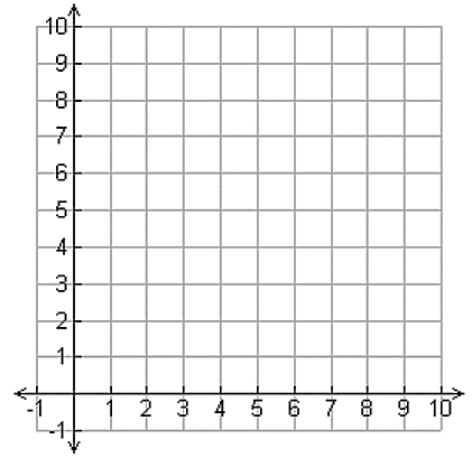
Calculate the slopes of all the sides.

$$m_{\overline{AB}} =$$

$$m_{\overline{BC}} =$$

$$m_{\overline{CD}} =$$

$$m_{\overline{DA}} =$$



Explain why $ABCD$ is a trapezoid:

Check to see if it is an isosceles trapezoid.

Method 1: Show legs are congruent.

Method 2: Show diagonals are congruent.

Find the lengths of the legs.

Find the lengths of the diagonals.

Distance Formula $d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$ or Pythagorean Theorem $a^2 + b^2 = c^2$

$$AD =$$

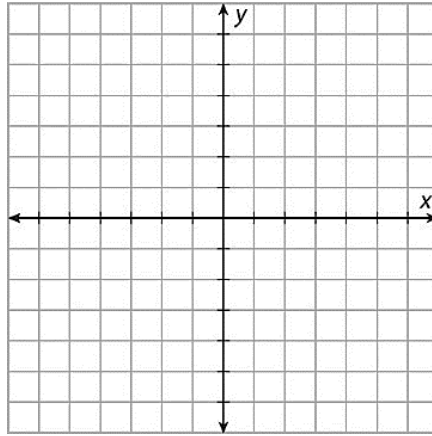
$$AC =$$

$$BC =$$

$$BD =$$

Explain why $ABCD$ is a trapezoid:

1. Prove that quadrilateral $A(-3, 3)$ $B(0, 5)$ $C(4, 1)$ $D(2, -2)$ is a trapezoid.



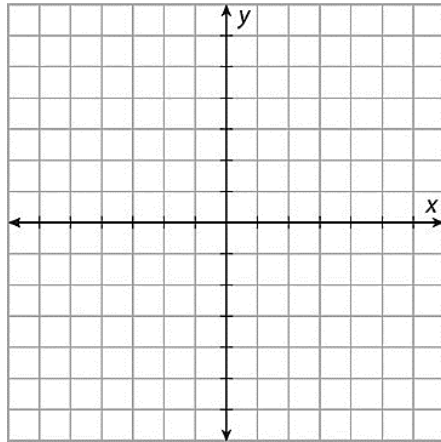
I know $ABCD$ is a trapezoid because _____

_____.

Is $ABCD$ an isosceles trapezoid? Why or why not? _____

_____.

2. Prove that quadrilateral $W(-4, 1)$ $X(-1, 4)$ $Y(6, 2)$ $Z(-1, -5)$ is a trapezoid.



I know $WXYZ$ is a trapezoid because _____

_____.

Is $WXYZ$ an isosceles trapezoid? Why or why not? _____

_____.