

Coordinate proof of a rhombus

Name _____

Use Coordinate Geometry to prove that parallelogram $ABCD$ is a rhombus given the vertices $A(2, 2)$, $B(4, 6)$, $C(8, 8)$ and $D(6, 4)$.

Method 1

Show that diagonals are perpendicular which means their slopes are opposite reciprocals. (or product is -1)

Formula for the slope $m = \frac{y_2 - y_1}{x_2 - x_1}$

Calculate the slopes of the diagonals.

$$m_{\overline{AC}} =$$

$$m_{\overline{BD}} =$$

Explain why $ABCD$ is a rhombus:

Method 2

Show that all sides are congruent which means they have the same length.

Find the lengths of the sides.

Distance Formula $d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$ or Pythagorean Theorem $a^2 + b^2 = c^2$

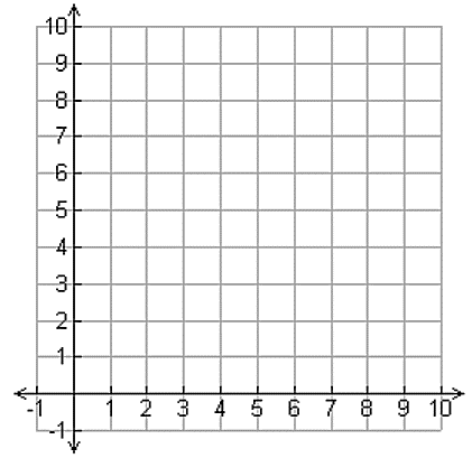
$$AB =$$

$$CD =$$

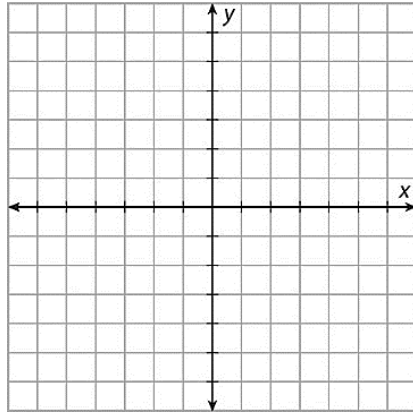
$$BC =$$

$$DA =$$

Explain why $ABCD$ is a rhombus:



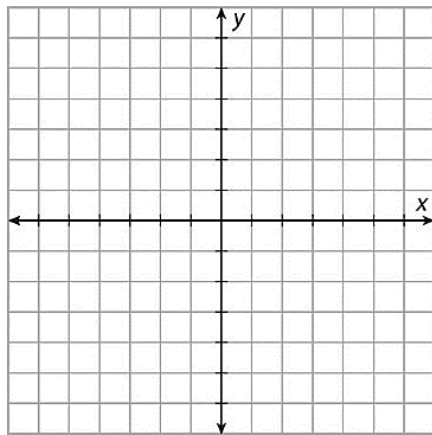
1. Prove that quadrilateral $A(-3, 2)$ $B(-2, 6)$ $C(2, 7)$ $D(1, 3)$ is a rhombus.



I know $ABCD$ is a parallelogram because _____

I know $ABCD$ is a rhombus because _____

2. Prove that quadrilateral $W(-3, 3)$ $X(2, 3)$ $Y(-2, 0)$ $Z(-7, 0)$ is a rhombus.



I know $WXYZ$ is a parallelogram because _____

I know $WXYZ$ is a rhombus because _____
